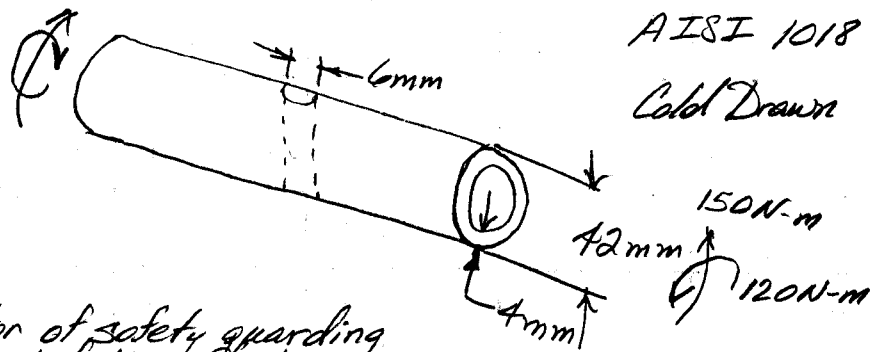


Given:



Find: Factor of safety guarding against fatigue failure.

Solution:

Reference Table A-16 for bending stress concentration factor.

$$\frac{a}{D} = \frac{6}{42} = 0.142 \quad \frac{d}{D} = \frac{34}{42} = 0.81$$

$$A \approx 0.79 \quad K_t \approx 2.39$$

$$Z_{net} = \frac{\pi A}{32D} (D^4 - d^4)$$

$$= \frac{\pi (0.79)}{32 (0.042)} (0.042^4 - 0.034^4)$$

$$= 3.28 \times 10^{-6} \text{ m}^3$$

$$\sigma_{ob} = \frac{M}{Z_{net}} = \frac{150 \text{ N-m}}{3.28 \times 10^{-6} \text{ m}^3} = 45.8 \text{ MPa}$$

Reference TABLE A-16 for torsional stress concentration factor.

$$A = 0.89 \quad K_{ts} = 1.75$$

$$J_{net} = \frac{\pi A (D^4 - d^4)}{32} = \frac{\pi (0.89) (0.042^4 - 0.034^4)}{32}$$

$$= 1.55 \times 10^{-9} \text{ m}^4$$

$$\tau_0 = \frac{TD}{2J_{net}} = \frac{(120 \text{ N}\cdot\text{m})(0.042 \text{ m})}{2(1.55 \times 10^{-9} \text{ m}^4)}$$

$$= 16.3 \text{ MPa}$$

From Figure 5-16, the notch sensitivity can be estimated to be $q = 0.8$.

$$\Rightarrow K_{fb} = 1 + q(K_t - 1)$$

$$= 1 + 0.8(2.39 - 1) = 2.1$$

$$K_{fs} = 1 + q(K_{ts} - 1) = 1.6$$

$$\Rightarrow \sigma_b = 45.8 \text{ MPa}(2.1) = 96.2 \text{ MPa}$$

$$\tau_s = 16.3 \text{ MPa}(1.6) = 26.1 \text{ MPa}$$

Compute principal stresses.

$$\begin{aligned}\sigma_1 &= \frac{\sigma_{xx} + \sigma_{yy}}{2} + \sqrt{\left(\frac{\sigma_{xx} - \sigma_{yy}}{2}\right)^2 + \tau_{xy}^2} \\ &= \frac{96.2}{2} + \sqrt{\left(\frac{96.2}{2}\right)^2 + 26.1^2} \\ &= 103 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\sigma_2 &= \frac{\sigma_{xx} + \sigma_{yy}}{2} - \sqrt{\left(\frac{\sigma_{xx} - \sigma_{yy}}{2}\right)^2 + \tau_{xy}^2} \\ &= \frac{96.2}{2} - \sqrt{\left(\frac{96.2}{2}\right)^2 + 26.1^2} \\ &= -6.62 \text{ MPa}\end{aligned}$$

Accounting for third axis and ordering in highest to lowest order yields

$$\sigma_1 = 103 \text{ MPa}, \sigma_2 = 0, \sigma_3 = -6.62 \text{ MPa}$$

Compute von Mises stress

$$\begin{aligned}\sigma_{\text{eff}} &= \sqrt{\frac{(\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_3 - \sigma_1)^2}{2}} \\ &= \sqrt{\frac{(103)^2 + (-6.62)^2 + (109.6)^2}{2}} \\ &= \underline{\underline{106 \text{ MPa}}}\end{aligned}$$

From TABLE A-20, $S_{ut} = 440 \text{ MPa}$.

$$S_e' = 0.5 S_{ut} = 220 \text{ MPa}$$

Compute Marin factors

$$k_a = a S_{ut}^b \quad \text{from Table 7-4, } a = 2.70, b = -0.265$$

$$k_a = 2.70(440)^{-0.265} = 0.538$$

$$k_b = \left(\frac{D}{7.62}\right)^{-0.1133} = \left(\frac{42}{7.62}\right)^{-0.1133} = 0.824$$

$$k_c = k_d = 1.0$$

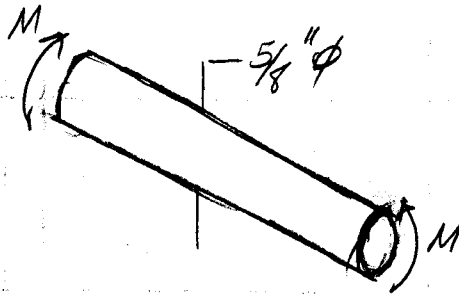
$$\Rightarrow S_e = (0.538)(0.824)(1.0)(1.0) 220 \text{ MPa} \\ = 97.5 \text{ MPa.}$$

Since the endurance limit is less than the effective alternating stress, there is no safety factor for infinite life

$$\frac{106 \text{ MPa}}{97.5 \text{ MPa}} = \frac{1}{N_f}$$

$\Rightarrow N_f = 0.92$. \Rightarrow part will have less than infinite life, finite life estimate is required.

Given:



$$M_1 = 1200 \text{ in-lb}, n_1 = 2,000$$

$$M_2 = 1000 \text{ in-lb}, n_2 = 100,000$$

$$M_3 = 900 \text{ in-lb}, n_3 = 10,000$$

Find: Determine whether bar will fail due to fatigue.

Solution:

$$I = \frac{\pi}{64} D^4 = \frac{\pi}{64} (0.625)^4 = 7.49 \times 10^{-3} \text{ in}^4$$

$$C = \frac{0.625 \text{ in}}{2} = 0.3125 \text{ in}$$

$$\sigma_1 = \frac{M_1 C}{I} = \frac{(1200 \text{ in-lb})(0.3125)}{7.49 \times 10^{-3}} = \underline{\underline{50 \text{ ksi}}}$$

$$\sigma_2 = \frac{M_2 C}{I} = \left(\frac{1,000 \text{ in-lb}}{1,200 \text{ in-lb}} \right) (50 \text{ ksi}) = \underline{\underline{41.7 \text{ ksi}}}$$

$$\sigma_3 = \frac{M_3 C}{I} = \left(\frac{900 \text{ in-lb}}{1,200 \text{ in-lb}} \right) (50 \text{ ksi}) = \underline{\underline{37.5 \text{ ksi}}}$$

From Fig. 7-6, at σ_1 , $N_1 = 57,000$ cycles

$S_{ult} = 116 \text{ ksi}$

Use Eq. 7-7 \Rightarrow at σ_2 , $N_2 = 160,000$ cycles

to estimate at σ_3 , $N_3 = 280,000$ cycles

Using Miner's rule,

$$\frac{2,000}{57,000} + \frac{100,000}{160,000} + \frac{19,000}{280,000} = \underline{\underline{0.70}}$$

⇒ Part will not fail.

Given: Same as problem #2 except an axial force of 5,000 lb is also acting on the bar.

Find: Determine whether bar will fail due to fatigue.

Solution:

$$\sigma_m = \frac{P}{A} \quad \text{Area} = \frac{\pi}{4} D^2 = \frac{\pi}{4} (0.625 \text{ in})^2$$
$$= 0.307 \text{ in}^2$$

$$\Rightarrow \sigma_m = \frac{5,000 \text{ lb}}{0.307 \text{ in}^2} = 16.3 \text{ ksi}$$

Find equivalent alternating stress for
 $\sigma_a = 50 \text{ ksi}$, $\sigma_m = 16.3 \text{ ksi}$.

$$\frac{\sigma_a}{\sigma_{eqv}} + \frac{\sigma_m}{S_{ut}} = 1$$

$$\Rightarrow \frac{\sigma_a}{\sigma_{eqv}} = 1 - \frac{\sigma_m}{S_{ut}}$$

$$\Rightarrow \sigma_{eqv} = \frac{\sigma_a}{1 - \frac{\sigma_m}{S_{ut}}}$$

$$\Rightarrow \sigma_{eqv} = \frac{50 \text{ ksi}}{\left(1 - \frac{16.3 \text{ ksi}}{116 \text{ ksi}}\right)} = \underline{\underline{58.2 \text{ ksi}}}$$

Find equivalent alternating stress for

$$\sigma_a = 41.7 \text{ ksi}, \quad \sigma_m = 16.3 \text{ ksi}$$

$$\sigma_{eq2} = \frac{41.7}{\left(1 - \frac{16.3}{116}\right)} = 48.5 \text{ ksi}$$

Find equivalent alternating stress for

$$\sigma_a = 37.5 \text{ ksi}, \quad \sigma_m = 16.3 \text{ ksi}$$

$$\sigma_{eq3} = \frac{37.5 \text{ ksi}}{\left(1 - \frac{16.3}{116}\right)} = 43.6 \text{ ksi}$$

From Fig. 7-6, $S_{ult} = 116 \text{ ksi}$, Use eq. 7-7 to find cycles

$$\text{at } \sigma_{eq1} = 58.2 \text{ ksi}, \quad N_1 = 3,000 \text{ cycles}$$

$$\text{at } \sigma_{eq2} = 48.5 \text{ ksi}, \quad N_2 = 29,000 \text{ cycles}$$

$$\text{at } \sigma_{eq3} = 43.6 \text{ ksi}, \quad N_3 = 90,000 \text{ cycles}$$

Using Minor's

$$\frac{2,000}{25,000} + \frac{100,000}{70,000} + \frac{10,000}{120,000} = 1.59$$

\Rightarrow Part will fail due to fatigue