

Given: Pinion Gear
 6 teeth/in 60 teeth
 22 teeth
 20° pressure angle
 1800 rpm
 15 hp
 face = 2 in.

Find: Estimate for bending stress.

Solution: The AGMA bending stress equation is

$$\sigma = \frac{W_t P_d}{F J} * K_a * K_s * K_m * K_v$$

The torque may be found from

$$T = 63,000 \frac{P}{n}$$

$$= 63,000 \left(\frac{15 \text{ hp}}{1800 \text{ rpm}} \right) = 787.5 \text{ in-lb}$$

The pitch diameter can be found from

$$P_d = \frac{N}{d} = 6 = \frac{22}{d} \Rightarrow d = \frac{22}{6} = 3.66 \text{ in}$$

The transmission force W_t can be found

$$\text{from } W_t = \frac{T}{(d/2)} = \frac{787.5 \text{ in-lb}}{(3.66 \text{ in}/2)} = \underline{\underline{430.3 \text{ lb}}}$$

The form factor, J , can be found from the chart in the lecture notes, or Shigley Fig 14-4

$$J \approx 0.35$$

$\frac{1}{K_v}$ can be found from figure 14-7 in Shigley.

The pitch line velocity is given by

$$V = r\omega$$

$$V = \left(1200 \frac{\text{rev}}{\text{min}}\right) \left(\frac{2\pi \text{ rad}}{\text{rev}}\right) \left(\frac{3.66 \text{ in}}{2}\right) \left(\frac{\text{ft}}{12 \text{ in}}\right)$$

$$= 1,150 \text{ ft/min}$$

The quality factor is chosen to be 8,

$$\Rightarrow \frac{1}{K_v} = 0.8$$

K_m is found from Table 14-6. For a medium rigidity mounting, $K_m = 1.6$

K_a and K_s are taken to be 1.

$$\Rightarrow \sigma \approx \frac{(430.316)(6)}{(2)(0.35)} \left(\frac{1}{0.8}\right) (1.6)(10)(10)$$

$$\sigma = \underline{\underline{7,400 \text{ psi}}}$$

Given: Pinion

$$\text{module} = 1.25 \text{ mm} = \frac{d}{N}$$

$$N = 18$$

$$\phi = 20^\circ$$

$$F = 12 \text{ mm}$$

$$n = 1800 \text{ rev/min}$$

$$P = 0.5 \text{ kW}$$

Find: Bending stress

Solution:

The power is given by

$$P = T\omega$$

$$\Rightarrow T = \frac{P}{\omega} = \frac{(0.5 \text{ kW}) \left(\frac{10^3 \text{ W}}{\text{kW}} \right) \left(\frac{\text{N}\cdot\text{m}}{\text{S}\cdot\text{W}} \right)}{(1800 \text{ rev/min}) \left(\frac{\text{min}}{60 \text{ sec}} \right) \left(\frac{2\pi \text{ rad}}{\text{rev}} \right)}$$

$$= 2.65 \text{ N}\cdot\text{m}$$

The pitch diameter can be found from the module and number of teeth

$$\Rightarrow d = N \cdot m = 18 (1.25 \text{ mm}) = 22.5 \text{ mm}$$

$$\text{The tooth load force } W_t = \frac{T}{(d/2)} = \frac{2.65 \text{ N}\cdot\text{m}}{(0.0225/2 \text{ m})}$$

$$W_t = 236 \text{ N}$$

The AGMA equation is

$$\sigma = \frac{W_t P_d}{F J} * K_a * K_s * K_m * K_v$$

The geometry factor is estimated to be
 $J = 0.3$ from Figure 14-4.

The pitch line velocity is obtained
 from

$$V = r \omega$$

$$= \left(\frac{0.0225}{2} \text{ m} \right) \left(1800 \frac{\text{rev}}{\text{min}} \right) \left(\frac{\text{min}}{60 \text{ sec}} \right) \left(\frac{2\pi \text{ rad}}{\text{rev}} \right)$$

$$= 2.12 \text{ m/s}$$

From Figure 14-7, $1/K_v \approx 0.9$

$$\Rightarrow K_v = \frac{1}{0.9} = 1.111$$

From Figure 14-6, $K_m \approx 1.6$

$$\Rightarrow \sigma = \frac{(236 \times \frac{1}{0.00125}) (1.111)(1.6)}{(0.012)(0.3)}$$

$$= 93.2 \text{ MPa}$$